

Anna Adarsh College for Women

Statistics - II

Answer Key

Section - B.

13) (i) $P(A) = \frac{1}{6}$

(ii) $P(A) = \frac{5}{36}$

14) $P(H) = \frac{1}{2}$ $P(T) = \frac{1}{2}$

$$P(X) = {}^{10}C_x \left(\frac{1}{2}\right)^x \left(\frac{1}{2}\right)^{10-x} = {}^{10}C_x \left(\frac{1}{2}\right)^{10}$$

$$P(X \geq 7) = P(X=7) + P(X=8) + P(X=9) + P(X=10)$$

$$= \left(\frac{1}{2}\right)^{10} [{}^{10}C_7 + {}^{10}C_8 + {}^{10}C_9 + {}^{10}C_{10}]$$

$$P(X \geq 7) = \frac{176}{1024}$$

15) $P(X \geq 20)$ when $\alpha = 20$ $Z = \frac{20 - 12}{4} = 2$

$$\therefore P(X \geq 20) = P(Z \geq 2) = 0.5 - P(0 \leq Z \leq 2)$$

$$= 0.5 - 0.4772$$

$$= 0.0228$$

16) $n = 22$, $\bar{x} = 153.7$, $s = 17.2$

$$H_0: \mu > 146.3 \quad t = \frac{\bar{x} - \mu}{\frac{s}{\sqrt{n-1}}} = 9.03 \quad T.V = 17.2$$

Reject H_0 ; Advertising Campaign was successful

$$17) E_1 = 1440 \quad E_2 = 5760$$

$$E_3 = 4160 \quad E_4 = 640$$

$$\chi^2 = 13.89$$

$$T.V = 3.84$$

Distinction is made in appointment on the basis of Gender.

18) Chi-Square Distribution - Explanation..

$$19) n = 1000 \quad x = 540$$

$$p = \frac{540}{1000} = 0.540$$

$$P = 0.5 \quad Q = 0.5$$

$$H_1: P \neq 0.5$$

$$Z = \frac{p - P}{\sqrt{PQ/n}} = 2.532$$

$$T.V = 2.58$$

Rice and wheat rates are equally popular in the

Section - C.

$$20) \text{ (i) } \frac{{}^6C_2 \times {}^{13}C_1}{{}^{19}C_3}$$

$$\text{ (ii) } \frac{{}^6C_1 + {}^4C_1 + {}^9C_1}{{}^9C_3}$$

$$\text{(iii)} \quad \frac{{}^{15}C_3}{{}^{19}C_3}$$

$$\text{(iv)} \quad 1 - \frac{{}^{13}C_3}{{}^{19}C_3}$$

$$21) \quad N = 100 \quad n = 500 \quad p = 0.01 \quad \lambda = np = 0.5$$

$$f(x) = N \cdot P(x) = \frac{100 \times 0.6065 \times (0.5)^x}{x!}$$

$$\text{(i) No Defective} = 100 \times P(x=0) = 100 \times 0.6065 \\ \approx 61 \text{ Bottles.}$$

(ii) at least two Defective.

$$= 100 [P(x \geq 2)] = 100 [1 - P(x=0) - P(x=1)] \\ = 100 [1 - 0.6065 - 0.6065 \times 0.5] \\ = 9.$$

$$22) \quad P(X < 25) = 0.1003 \text{ and } P(X < 70) = 0.8997$$

$$\text{when } x = 25 \quad Z = \frac{25 - \mu}{\sigma} = -Z_1$$

$$\text{when } x = 70 \quad Z = \frac{70 - \mu}{\sigma} = Z_2.$$

$$P(Z < -Z_1) = 0.1003$$

$$P(Z < Z_2) = 0.8997$$

$$25 - \mu = -1.286$$

$$70 - \mu = 1.286$$

$$\sigma = 17.578$$

$$\mu = 47.5$$

23)

$$\bar{x} = 50.875$$

$$\bar{y} = 52.875$$

$$\sum (x - \bar{x})^2 = 30.875$$

$$\sum (y - \bar{y})^2 = 16.875$$

$$s^2 = 3.41$$

$$t = 2.17$$

Food A and Food B Differ significantly.

24) $E(620) = 585$

$$E(380) = 417$$

$$E(550) = 585$$

$$E(450) = 415$$

$$M^2 = 10.089$$

$$T.V = 3.841$$

The nature of area is related to voting preference in the election.